

D)  $g(x) = e^{1-2x^2}$ ;  $g' = -4xe^{1-2x^2}$ ;  $g'' = 4(4x^2-1)e^{1-2x^2}$

I  $g$  is defined everywhere;  $g(x) > 0$ , and as  $1-2x^2 \leq 1$ ,  $g(x) \leq e^1 = e$ .  $g(0) = e$  so  $g$  has an absolute max. at 0  
 $g$  is symmetric and  $\lim_{x \rightarrow \pm\infty} g(x) = 0$  (since  $1-2x^2 \rightarrow -\infty$ )  
 The  $x$ -axis is a horizontal asymptote

II  $g'(x) = 0$  when  $x = 0$   
 $g'$ 

+		-
↗	0	↘

 $g$  has an max at  $x=0$

III  $g''(x) = 0$  when  $x = \pm \frac{1}{2}$   
 $g''$ 

+		-		+
∪	-1/2	∩	1/2	∪

 $g$  has inflection points at  $x = \pm \frac{1}{2}$

IV

$x$	0	$\pm 1/2$	$\pm 1$	$\pm 2$
$g(x)$	e 2.7 abs. max	1.6	.37	.0009

