INSTRUCTIONS: Answer the following questions in the spaces provided below.

1. Write the augmented matrix corresponding to the following system in the space to the [2]

 $\begin{cases} x_1 + 2x_2 &= -3x_3 + 4 \\ x_2 - 3x_3 &= 2 - 3x_1 \\ x_3 + x_1 &= 1 - 2x_2 \end{cases} \qquad \begin{bmatrix} 1 & 2 & 5 \\ 3 & 1 & -3 \\ 1 & 2 & 1 \end{bmatrix} \qquad \begin{bmatrix} 4 \\ 2 \\ 1 & 1 \end{bmatrix}$ 

2. Consider the following two augmented matrices. Below each, describe, in words or [2] symbols, the next elementary row operation to be performed on each, according to the method of Gaussian elimination with back substitution, as described in the textbook and in class. (Do not compute anything).

(a)  $\begin{bmatrix} 0 & 2 & 4 & 6 \\ 3 & 0 & 1 & 4 \\ 0 & 1 & 2 & 3 \end{bmatrix}$ 

(b)  $\begin{vmatrix} 1 & 0 & 2 & -1 & 3 \\ 0 & 0 & 1 & 2 & 3 \\ 0 & 0 & -3 & 1 & 2 \end{vmatrix}$ 

 $R_1 \hookrightarrow R_2$ 

Rz CRz+3Rz

The following matrix is the reduced row echelon form of a system of linear equations [2] with variables x, y, z. Write the general solution of the system in the space to the right.

 $\begin{bmatrix} 1 & 0 & 4 & | & -3 \\ 0 & 1 & -2 & | & 1 \\ 0 & 0 & 0 & | & 0 \end{bmatrix}$   $\Rightarrow \text{set } 2 = t$  2 is fine:  $\Rightarrow \text{set } 2 = t$   $\Rightarrow \text{set } 3 = t$   $\Rightarrow \text{set } 3 = t$   $\Rightarrow \text{set } 3 = t$   $\Rightarrow \text{set } 4 = t$  [4]calculate it if it is defined, and explain why it is not defined otherwise.

(a) 2A + 3B

NOT DEFINED: 2A and 3B have different shapes

5. Let  $A = \begin{bmatrix} 3 & -1 & 4 \\ -1 & 5 & -9 \end{bmatrix}$  and  $B = \begin{bmatrix} -2 & 7 \\ 1 & 8 \\ 2 & -8 \end{bmatrix}$ . Find column 1 of AB. [2]