

NAME SOLUTIONS. ID Number \_\_\_\_\_

INSTRUCTIONS: Answer the following questions in the spaces provided below.

[12] TOTAL

- [2] 1. Write the augmented matrix corresponding to the following system in the space to the right:

$$\begin{cases} x_1 = 2x_2 - 3x_3 + 4 \\ x_2 = -x_3 + 2 + 3x_1 \\ x_3 = 1 + 3x_2 - 2x_1 \end{cases}$$

$$\left[ \begin{array}{ccc|c} 1 & -2 & 3 & 4 \\ -3 & 1 & 1 & 2 \\ 2 & -3 & 1 & 1 \end{array} \right]$$

- [2] 2. Consider the following two augmented matrices. Below each, describe, in words or symbols, the
- next*
- elementary row operation to be performed on each, according to the method of Gaussian elimination with back substitution, as described in the textbook and in class. (Do not compute anything).

$$(a) \left[ \begin{array}{ccc|c} 1 & -2 & 3 & -4 \\ 0 & 2 & -3 & 5 \\ 0 & 3 & 6 & 9 \end{array} \right]$$

$$(b) \left[ \begin{array}{cccc|c} 1 & -1 & 3 & -2 & 5 \\ 0 & 0 & 1 & 2 & 4 \\ 0 & 0 & 0 & 0 & 0 \end{array} \right]$$

$$\frac{1}{2}R_2$$

$$R_1 \leftarrow R_1 - 3R_2$$

- [2] 3. The following matrix is the reduced row echelon form of a system of linear equations with variables
- $x, y, z$
- . Write the general solution of the system in the space to the right.

$$\left[ \begin{array}{ccc|c} 1 & -3 & 0 & 2 \\ 0 & 0 & 1 & -4 \\ 0 & 0 & 0 & 0 \end{array} \right]$$

$y$  is free:  $y = t$ . Or:  $(x, y, z) = (2 + 3t, t, -4)$ .

$$\begin{cases} x = 2 + 3t \\ y = t \\ z = -4 \end{cases}$$

- [4] 4. Let
- $A = \begin{bmatrix} 2 & -1 & 3 \\ -3 & 2 & -1 \end{bmatrix}$
- and
- $B = \begin{bmatrix} 3 & -2 \\ 2 & -3 \\ 4 & 2 \end{bmatrix}$
- . For each of the following expressions, calculate it if it is defined, and explain why it is not defined otherwise.

(a)  $2A - B^T$

$$\begin{bmatrix} 1 & -4 & 2 \\ -6 & 0 & -3 \end{bmatrix}$$

(b)  $B + 3A$

NOT DEFINED.

 $B$  and  $3A$  have different shapes

- [2] 5. Let
- $A = \begin{bmatrix} 3 & -1 & 4 \\ -1 & 5 & -9 \end{bmatrix}$
- and
- $B = \begin{bmatrix} -2 & 7 \\ 1 & 8 \\ 2 & -8 \end{bmatrix}$
- . Find row 2 of
- $AB$
- .

$$[-11 \quad 105]$$