

THE UNIVERSITY OF MANITOBADATE: Oct. 22, 2002

MIDTERM EXAMINATION

DEPARTMENT & COURSE NO: 136.270TIME: 1 hourEXAMINATION: Calculus 3AEXAMINER: Dr. F. Ghahramani

NAME: (PRINT)_____

STUDENT NUMBER:_____

SIGNATURE:_____

(I understand that cheating is a serious offense)

INSTRUCTIONS TO THE STUDENT

This is a one-hour exam. There are 3 pages of questions and one blank page for rough work. Check now that you have all 3 pages of questions.. Answer all the questions in the spaces provided. If necessary, you may continue your work on the reverse sides of the pages but PLEASE INDICATE CLEARLY that your work continues and where the continuation may be found. DO NOT detach any question pages from the exam.

The point value of each question is indicated to the left of the question number. The maximum score possible is 60 points.

Please present your work CLEARLY and LEGIBLY, and use a pen (not red) or a dark pencil. **Justify your answers unless otherwise stated.**

NO CALCULATORS, TEXTS, NOTES OR OTHER AIDS ARE PERMITTED.

Values

1. The curve C is given by the equation $\vec{r}(t) = 3\sin t \vec{i} + 4\sin t \vec{j} + 5\cos t \vec{k}$;
- [4] (a) Find the length of the arc between the points corresponding to $t = 0$ and $t = 1$.
- [8] (b) Find the Frenet frame $\{\vec{T}, \vec{N}, \vec{B}\}$ at a point corresponding to the general parameter t .

Values

2. Determine which one of the following limits exists and which one does not exist. Find the value of the one that exists. **Justify your answers.**

[4] (a) $\lim_{(x,y) \rightarrow (0,0)} \frac{x + y^2}{x^2 + y^2}$

[4] (b) $\lim_{(x,y) \rightarrow (0,0)} \frac{2x^2 + y^2 + xy^2}{2x^2 + y^2}$

- [14] 3. The surface S has the equation $z = 2x^2 - y^2 + 2xy$ in the three dimensional space. Find the equations of the tangent plane and the normal line to S at the point $(1,2,2)$ on S .

Values

[13] 4. Let $f(x,y,z) = y^3 e^x + xz^2$. Find $\frac{\partial^2 f}{\partial z \partial x}$ and $f_{3,1,2}$.

[13] 5. Let $z = ye^x - x^2$, $x = s^2 + t$, $y = s - t^2$. By using the **chain rule**, calculate $\frac{\partial z}{\partial t}$ and $\frac{\partial^2 z}{\partial s \partial t}$.

N.B. You will receive no credit if you attempt this question without using the chain rule.