

(f) $\lim_{x \rightarrow 0^+} (1-kx)^{\frac{1}{x}}$ is a " 1^∞ " indeterminate form. As an exponent is involved, we should start by computing the limit of the natural logarithm of the given expression.
Let $y = (1-kx)^{\frac{1}{x}}$. $\therefore \ln(y) = \frac{1}{x} \ln(1-kx)$.

$$\therefore \lim_{x \rightarrow 0^+} \ln(y) = \lim_{x \rightarrow 0^+} \frac{\ln(1-kx)}{x} \quad \text{This is an } \frac{0}{0} \text{ indeterminate form, so}$$

we use L'Hopital's rule to evaluate it.

$$= \lim_{x \rightarrow 0^+} \frac{\left(\frac{1}{1-kx}\right)(-k)}{1} = \lim_{x \rightarrow 0^+} \frac{-k}{1-kx} = -k.$$

$$\therefore \lim_{x \rightarrow 0^+} \ln(y) = -k.$$

$$\therefore \lim_{x \rightarrow 0^+} (1-kx)^{\frac{1}{x}} = \lim_{x \rightarrow 0^+} e^{\ln y} = e^{\lim_{x \rightarrow 0^+} \ln y}$$

↓ because the exponential function is continuous

$$= e^{-k}$$

2. C has parametric equations $x = 2 \sin\left(\frac{\pi t}{2}\right)$,
 $y = 3 \cos\left(\frac{\pi t}{2}\right)$, for $0 \leq t \leq 2$.

(a)

t	x	y	t	x	y	t	x	y
0	0	3	$\frac{2}{3}$	$\sqrt{3}$	$\frac{3}{2}$	$\frac{3}{2}$	$\sqrt{2}$	$-\frac{3}{\sqrt{2}}$
$\frac{1}{3}$	1	$\frac{3\sqrt{3}}{2}$	1	2	0	$\frac{5}{3}$	1	$-\frac{3\sqrt{3}}{2}$
$\frac{1}{2}$	$\sqrt{2}$	$\frac{3}{\sqrt{2}}$	$\frac{4}{3}$	$\sqrt{3}$	$-\frac{3}{2}$	2	0	-3