136.151: Test \#2 20 minutes

Name: $\qquad$

## Student Number:

$\qquad$

1. (a) Compute $\lim _{x \rightarrow \infty} \frac{x-1}{x+1}$. Write the equation of one horizontal asymptote of the function $f(x)=\frac{x-1}{x+1}$.
(b) Compute $\lim _{x \rightarrow-1^{-}} \frac{x-1}{x+1}$. Write the equation of one vertical asymptote of the function $f(x)=\frac{x-1}{x+1}$.
2. Compute $f^{\prime}(2)$ if $f(x)=3 x^{2}$ using ONLY the definition of the derivative of a function.
3. (a) Given $f(x)=\frac{\sqrt{x}}{x^{2}-1}$, compute $f^{\prime}(x)$. Use the rules of differentiation. Do not simplify your answer after differentiating.
(b) Suppose $x(t)=t^{3}-2 t$ is the distance measured in meters between a particle moving along the $x$-axis and the origin (with respect to the time $t$ measured in seconds). What is the acceleration at the moment when $t=2 \mathrm{sec}$ ?
