

B13.

**MATH 1300: Quiz #5**

Name \_\_\_\_\_

Student Number \_\_\_\_\_

1. (a) Consider the set  $S$  of all polynomials of type  $ax^2 + (2a - 3)x + b$ , where  $a$  and  $b$  range through the set of all real numbers. Is  $S$  a subspace of the vector space  $\mathcal{P}_2$  of all polynomials of degree at most 2? Justify your answer.

(b) Consider the set  $W$  of all triples of type  $(a, 0, b)$ , where  $a$  and  $b$  range through the set of all real numbers. Is  $W$  a subspace of the Euclidean vector space  $\mathbb{R}^3$ ? Justify your answer.

2. Let  $U$  be the subspace of the Euclidean vector space  $\mathbb{R}^3$  consisting of all triples of type  $(a, b, 0)$ , where  $a$  and  $b$  range through the set of all real numbers, and let  $S = \{(2, 0, 0), (0, 5, 0)\}$ . Show that  $\text{span}(S) = U$ .

3. Is the subset  $S = \{(1, 0, 0), (0, 1, 0), (1, 2, 3)\}$  of vectors in  $\mathbb{R}^3$  linearly independent? Justify your answer.