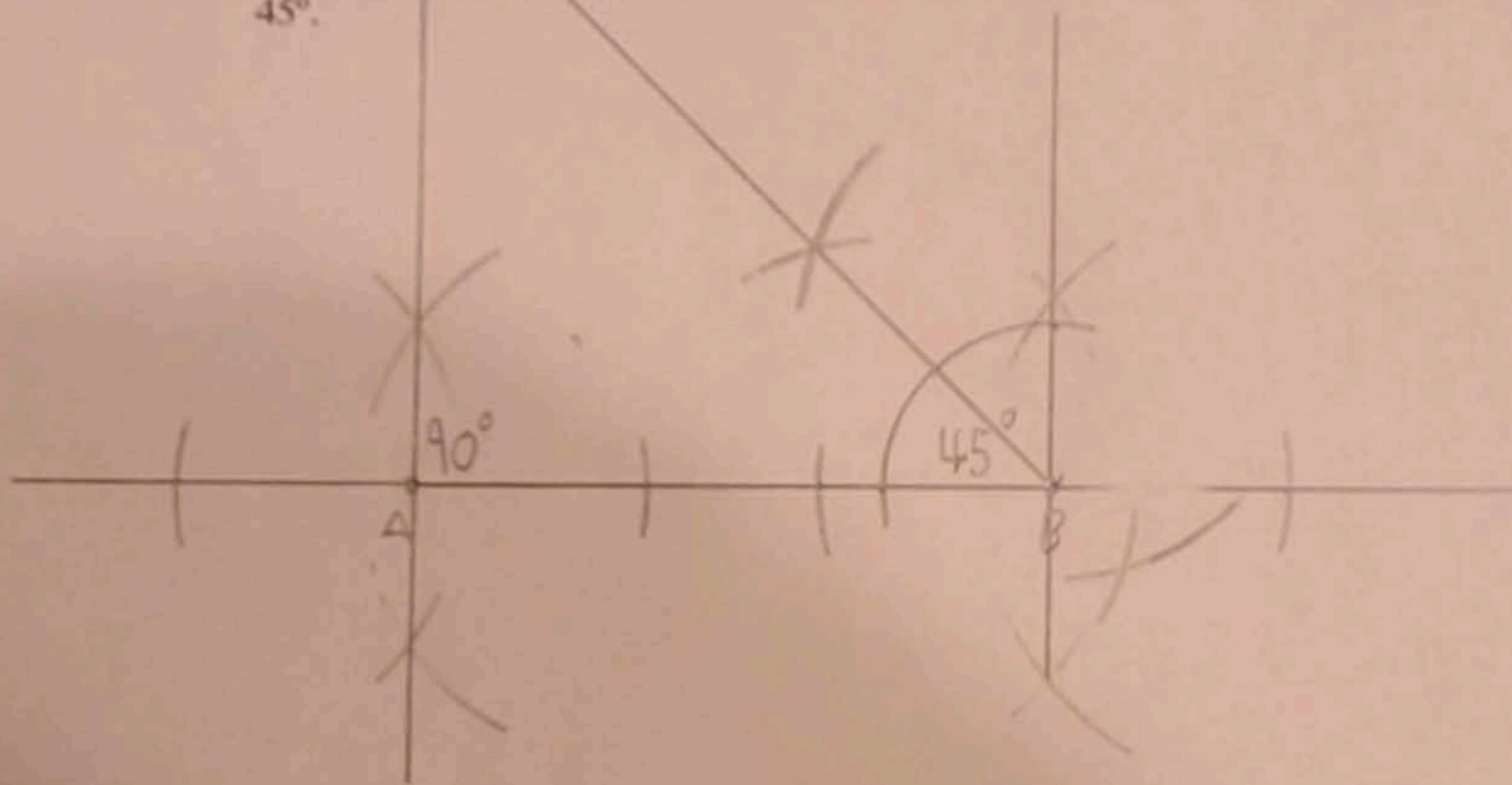
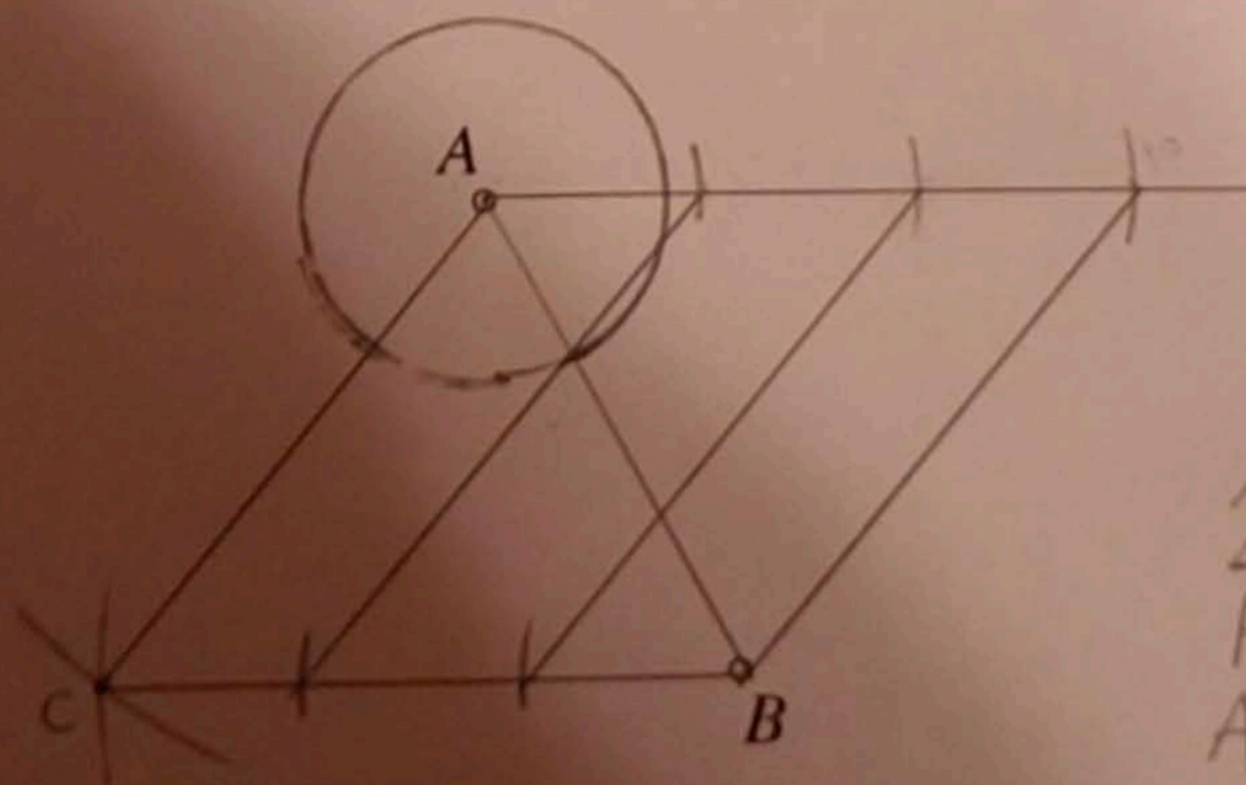


[9 points] 1. (a) [4] Construct a triangle where two of its interior angles are 90° and 45° .



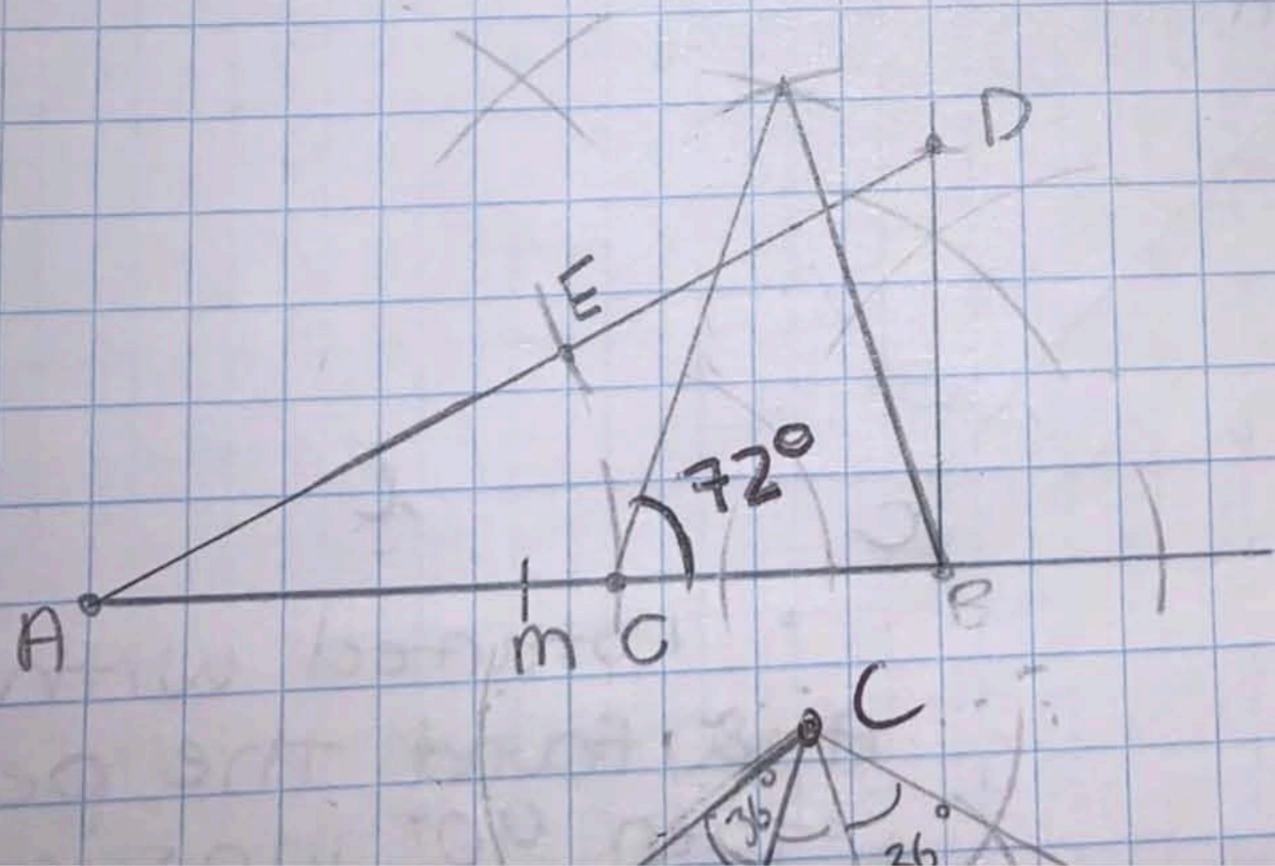
1. Begin with a line segment and mark point A and B
2. Create a perpendicular through both points
3. This gives us 2 90° angles. Divide one angle in half and connect the lines

(b) [5] The points A, B (to be shown) are given. Construct a circle centered at A and of radius $\frac{AB}{3}$. (Hint: subdivide AB into equal sub-segments.)

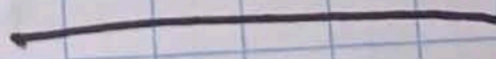


1. Create a new ray emanating from A and mark equal points. Connect the last point with B.
2. Construct a parallelogram centered on A, B. Mark the same distance on the parallel line. Connect the points
3. Draw a circle, sharp point on A, graphite on the $\frac{1}{3}$ marking.

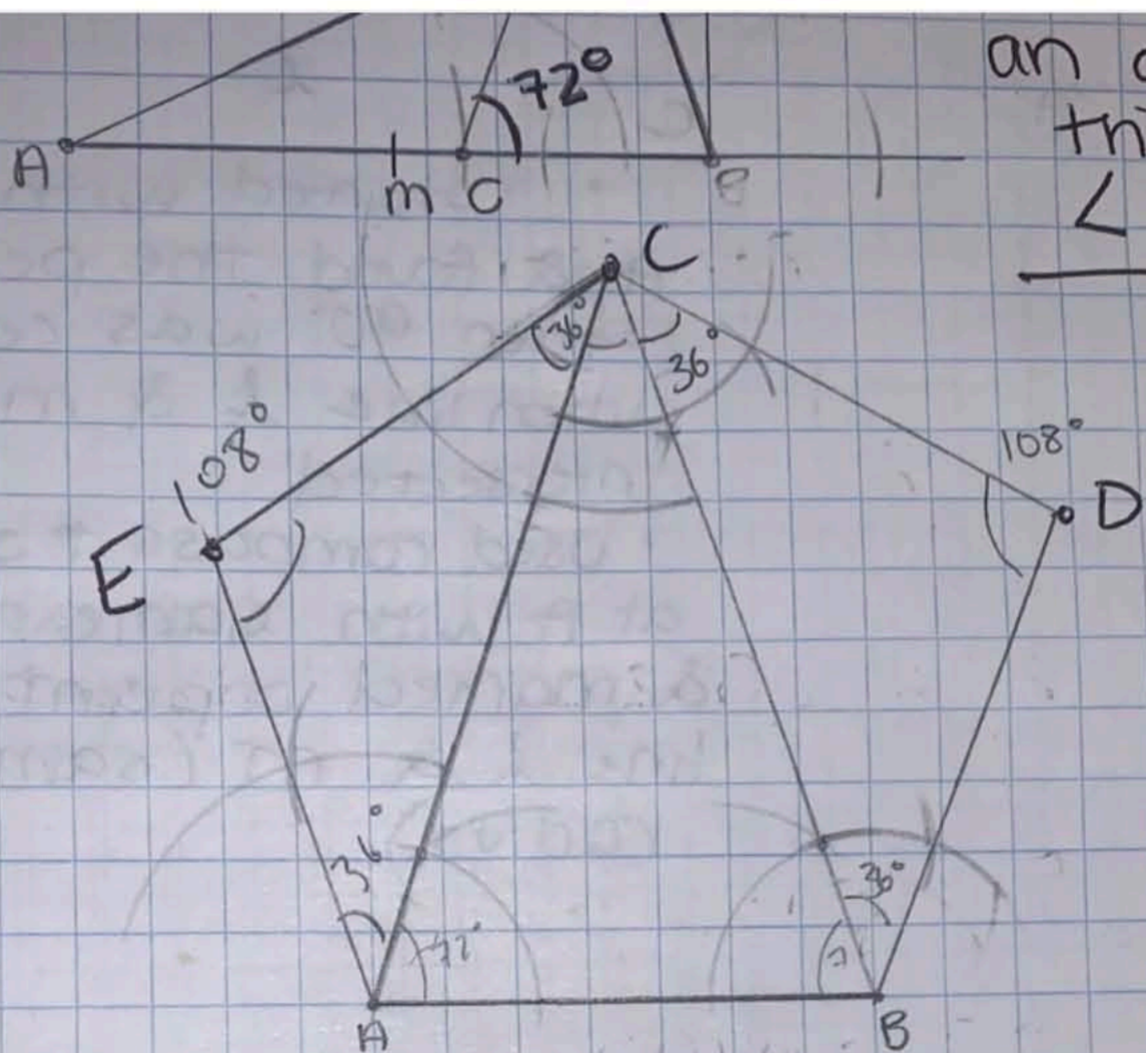
a)



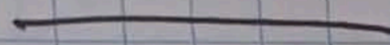
◦ I constructed a golden cut
 ◦ then constructed an acute golden triangle with $\angle 72^\circ$



b)

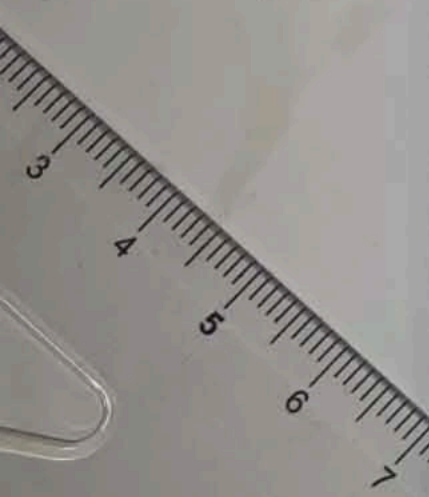


an acute golden triangle with $\angle 72^\circ$



◦ I duplicated acute golden triangle $\angle 72^\circ$ from Za's construction onto line AB & made acute golden triangle

◦ then I duplicate $\angle 36^\circ$ onto either side of point C, creating ~~acute~~ obtuse golden triangles with base AC & BC



Question 3.

a) the sequence of numbers $f_1, f_2, f_3, \dots, f_n$ is the fibonacci number sequence

if $f_1=1, f_2=1$ & $f_n = f_{n-1} + f_{n-2}$ for $n = 3, 4, 5, \dots$

b) $2f_{20} = 13530$ & $2f_{22} = 35422$. $f_{21} = ?$

$$2(f_{20}) + f_{21} = 2f_{22}$$

• I divided

a) the sequence of numbers $f_1, f_2, f_3, \dots, f_n$ is the fibonacci number sequence

if $f_1=1, f_2=1$ & $f_n = f_{n-1} + f_{n-2}$ for $n = 3, 4, 5, \dots$

b) $2f_{20} = 13530$ & $2f_{22} = 35422$. $f_{21} = ?$

$$\frac{2(f_{20}) + f_{21}}{2} = \frac{2f_{22}}{2}$$

$$\frac{13530 + f_{21}}{2} = \frac{35422}{2}$$

$$6765 + f_{21} = 17,711$$

$$f_{21} = 17,711 - 6765$$

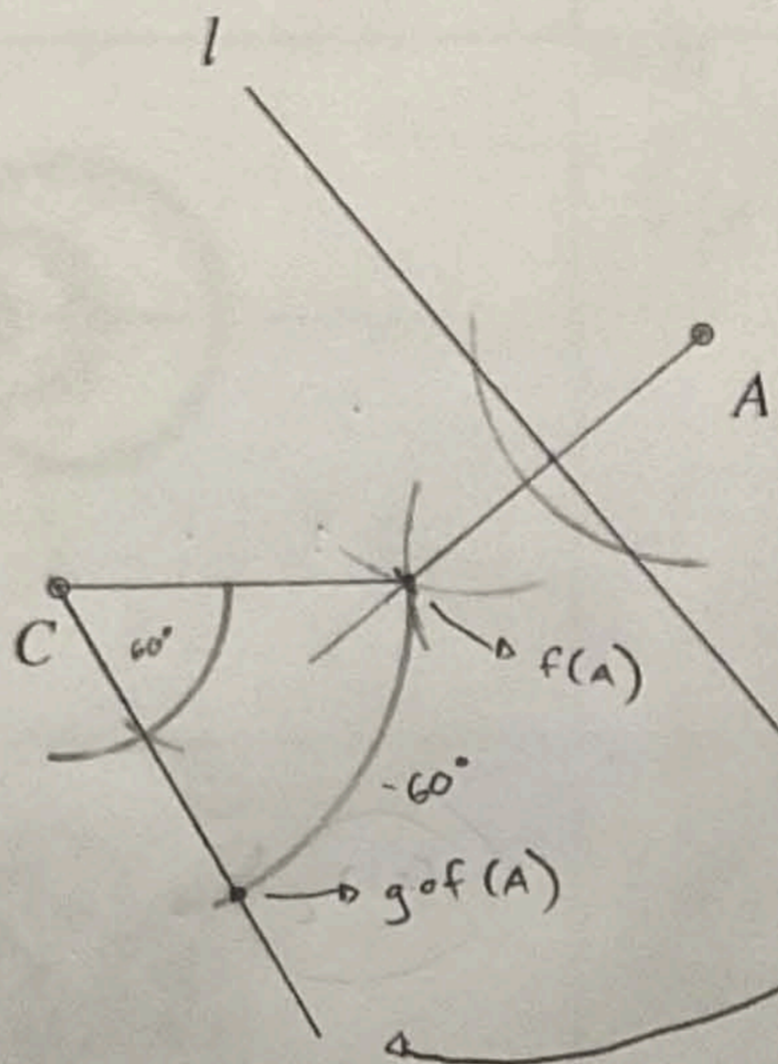
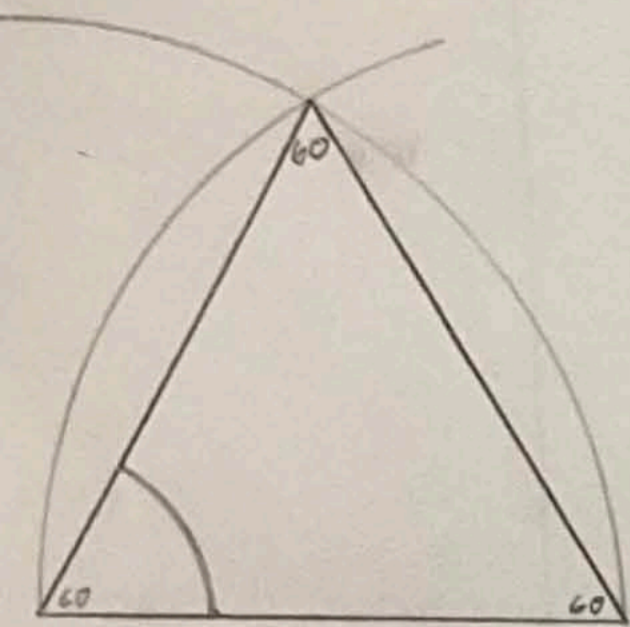
$$f_{21} = 10,946$$

• I divided f_{20} & f_{22} by 2 & finished the problem.

[10 points] 4. [6] (a) Find the image of the point A (shown below) under the composition $g \circ f$ of f followed by g , where f is the reflection with respect to the line l (shown below), and g is the rotation around the center C (shown below) through an angle of -60° .

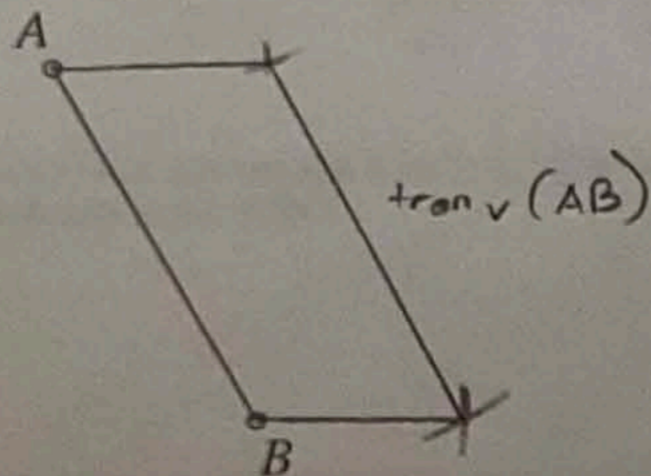
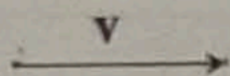
$$g \circ f(A) \quad f = \text{refl}$$

$$g = \text{rot}(C, -60^\circ)$$



- 1.) make perpendicular (A) towards line l ($f(A)$)
- 2.) connect C & $f(A)$
- 3.) construct equilateral triangle
- 4.) copy one angle \curvearrowright ; place towards point C
- 5.) make new line
- 6.) join $f(A)$ to new line to get $g \circ f(A)$ ✓

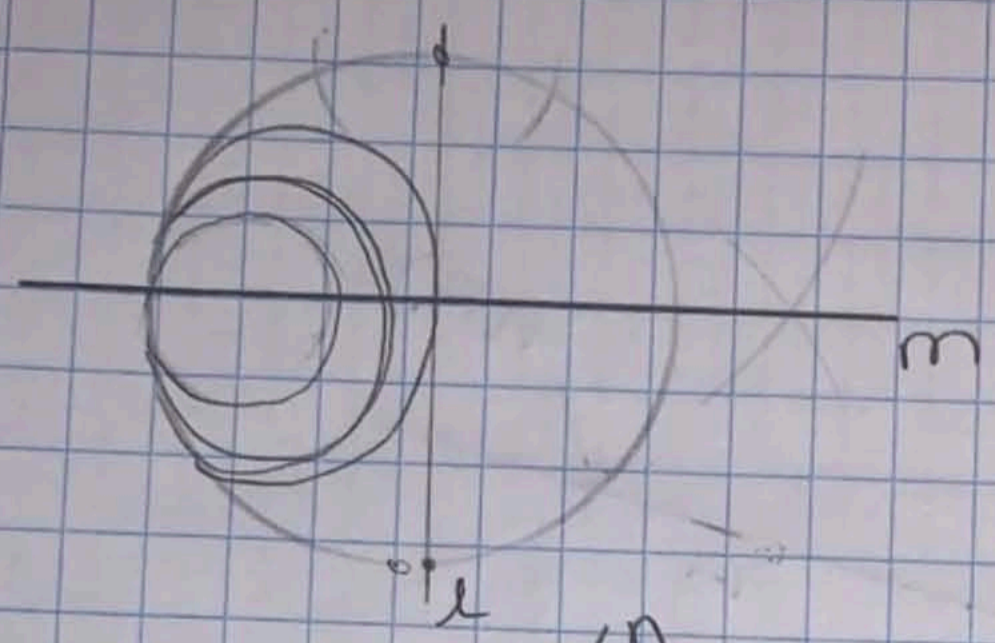
(b) [4] Construct the image of the line segment AB (shown below) under the translation with respect to the vector v (shown below).



- 1.) copy vector v length
- 2.) mark on arch, sharp point A
- 3.) copy distance between left end of v & point A
- 4.) mark on arch, sharp point right end of v & arch towards 1st arch ✓
- 5.) make parallelogram to obtain $(\text{tran } v(AB))$

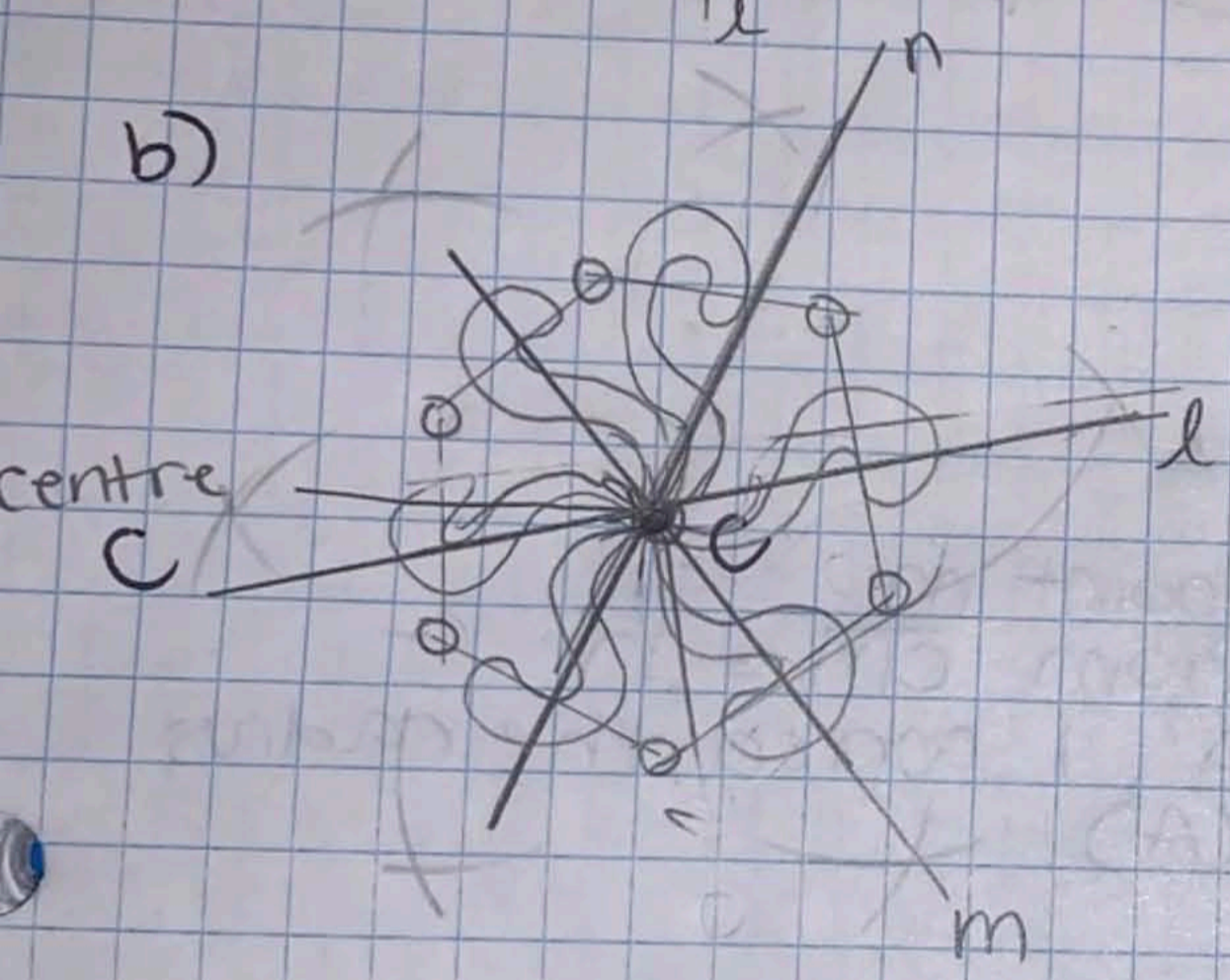
Question #5)

a)



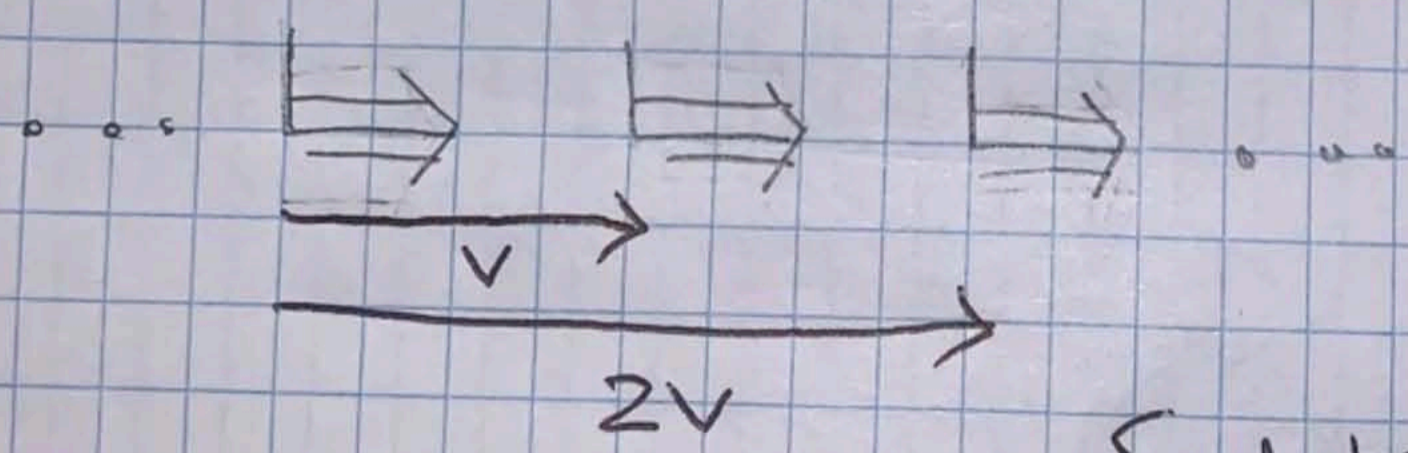
$$\{ id, \text{ref}_m \}$$

b)



$$\{ id, \text{rot}(C, 60^\circ), \text{rot}(C, 120^\circ), \text{rot}(C, 180^\circ), \text{rot}(C, 240^\circ), \text{rot}(C, 300^\circ) \}$$

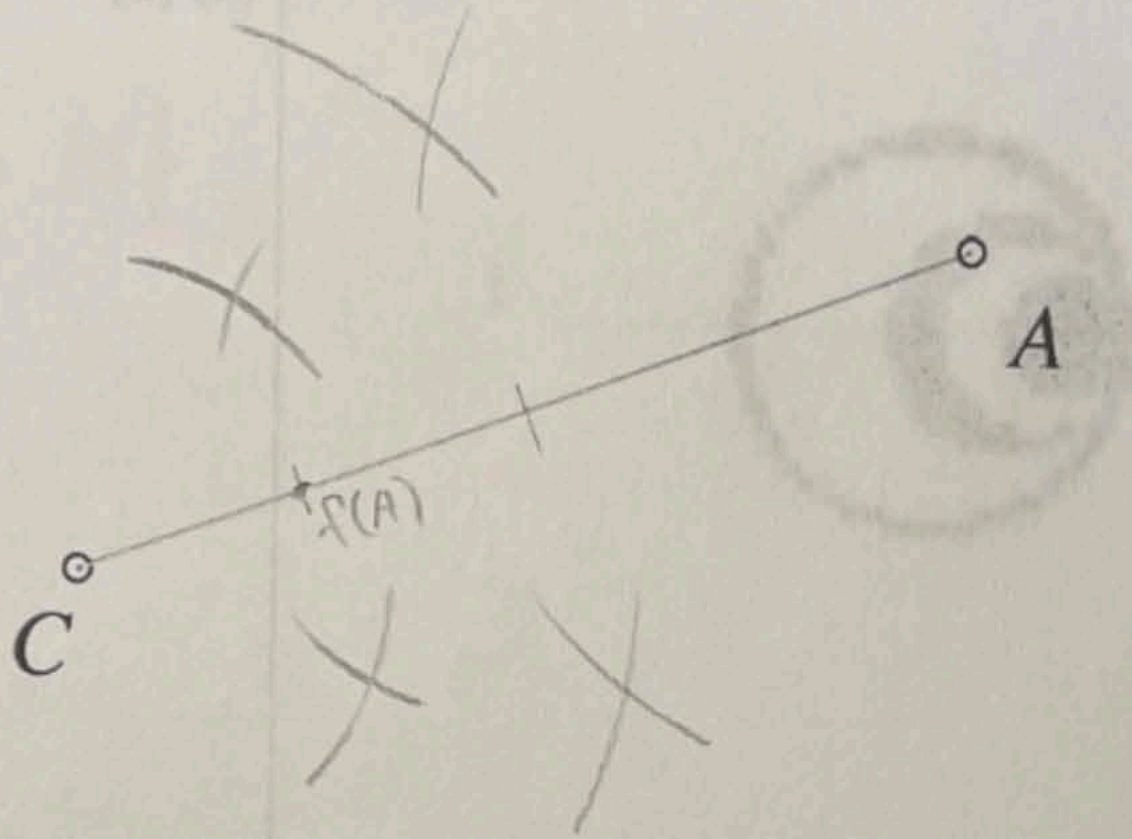
c)



$$\{ id, \text{tran}_v, \text{tran}_{2v}, \text{tran}_{3v}, \dots, \text{tran}_{-v}, \text{tran}_{-2v}, \text{tran}_{-3v}, \dots \}$$

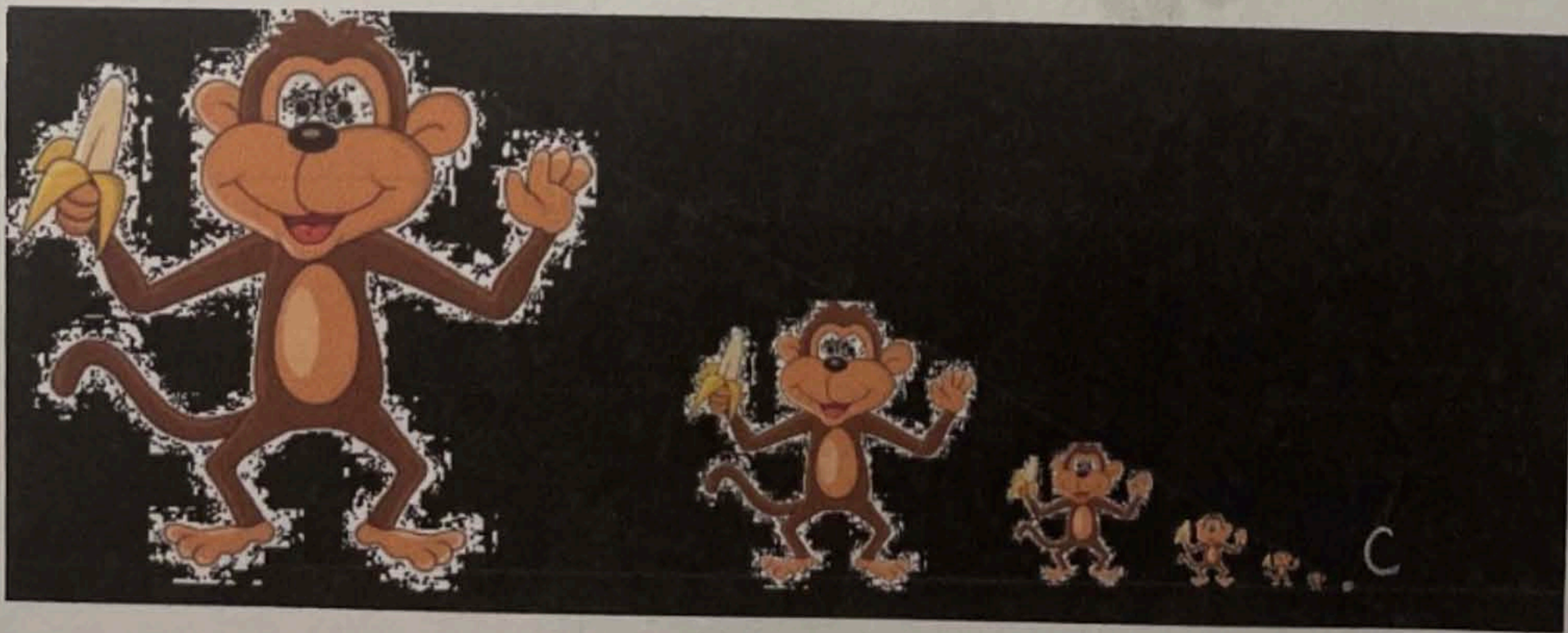
stretching factor $\alpha = \frac{1}{4}$. Construct the point $f(A)$ obtained by applying f to A . [You would need to construct the point $f(A)$ using a ruler and a compass!]

Subdivide CA into 4 using midpoint



Good 5

(b) [4] In the figure below every funny monkey every funny monkey except for the first one has a monkey twice its size immediately to the left of it. This pattern of monkeys continues without end, and the final outcome is a fractal called F . Confirm that the result is indeed a fractal: find a proper central similarity f that sends F within itself. You get the full mark if you indicate in the figure the center of your central similarity f , and write down the value of the stretching factor α of your central similarity.



centered at C

stretching factor $\alpha = \frac{1}{2}$

Good 4