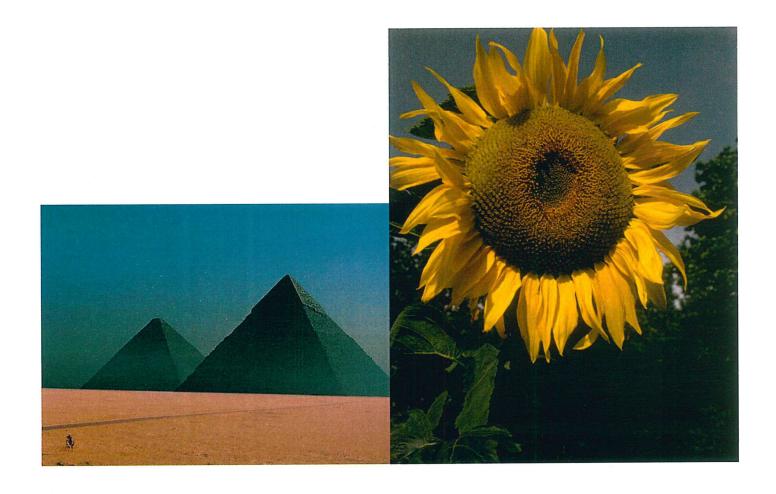
## Golden Ratio



#### The Golden Ratio

Given a line segment AB, the point C on the line such that the ratio of the length of the line AB to the length of the line AC is the same as



This ratio is known as the *Golden Ratio* and is denoted by the Greek letter  $\phi$ . We have

└ The Golden Ratio

$$\frac{AB}{AC} = \frac{AC}{CB} = \phi$$



#### Solutions To Quadratic Equations

An equation of the form:

$$ax^2 + bx + c = 0$$

has solutions

LThe Golden Ratio

#### The Value Of The Golden Ratio

#### The Value Of The Golden Ratio

Therefore

$$\phi = \frac{1+\sqrt{5}}{2} \approx 1.618$$

Note:  $\phi$  is the only positive solution to the equation

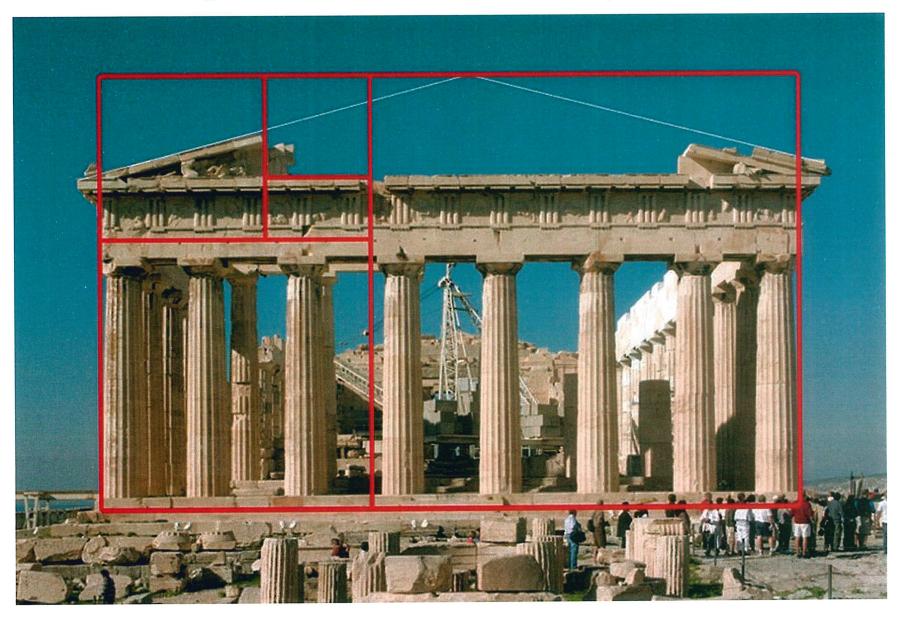
$$x^2 - x - 1 = 0$$
.

LThe Golden Ratio and Constructions

#### Construction 1: The Golden Cut

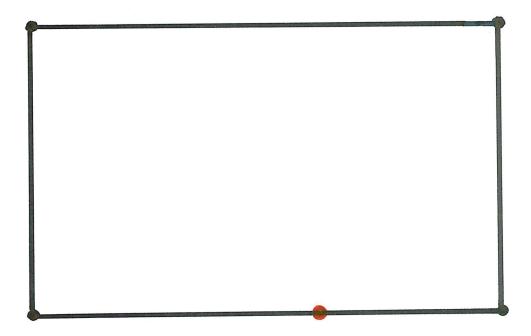


# Golden Rectangle: Parthenon, Athens (Built 448-432 BC.)



#### Golden Rectangle

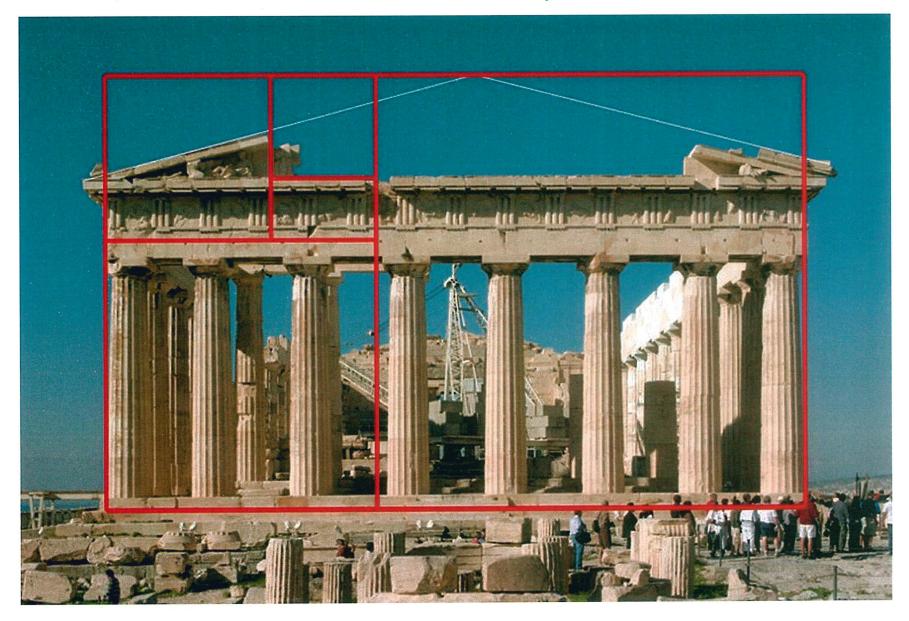
A Golden Rectangle is a rectangle that has side lengths that are in golden proportion.



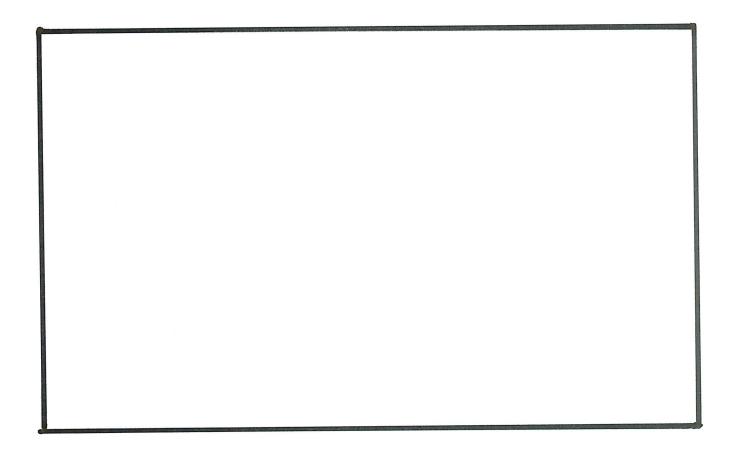
# Construction 2: Golden Rectangle Given A Shorter Side



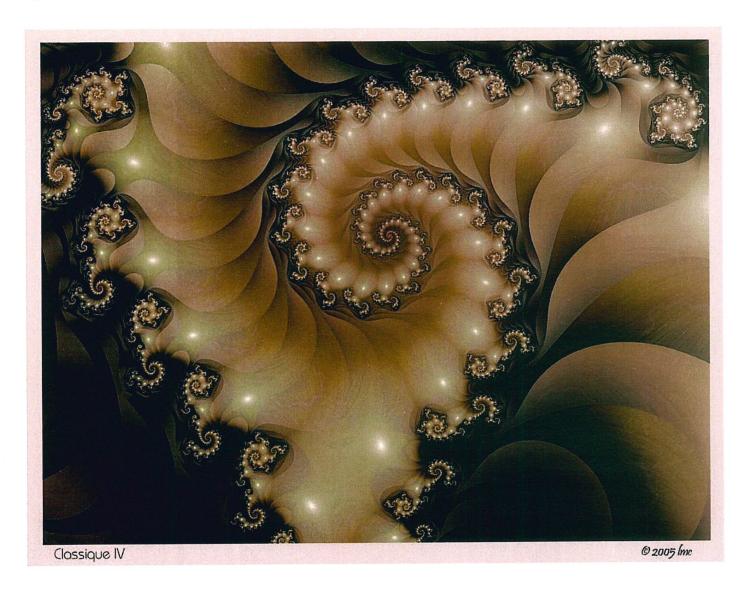
# Golden Spiral: Parthenon, Athens (Built 448-432 BC.)



## Construction 3: Golden Spiral

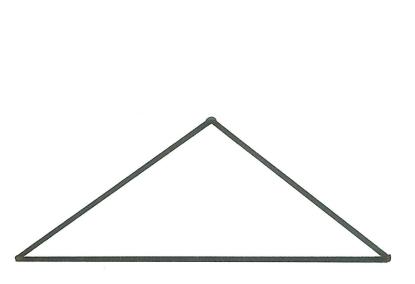


# Golden Spiral

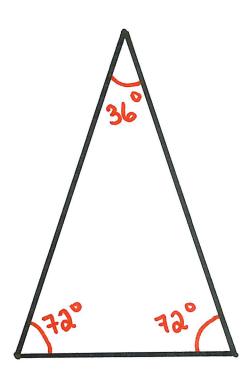


# Golden Triangles

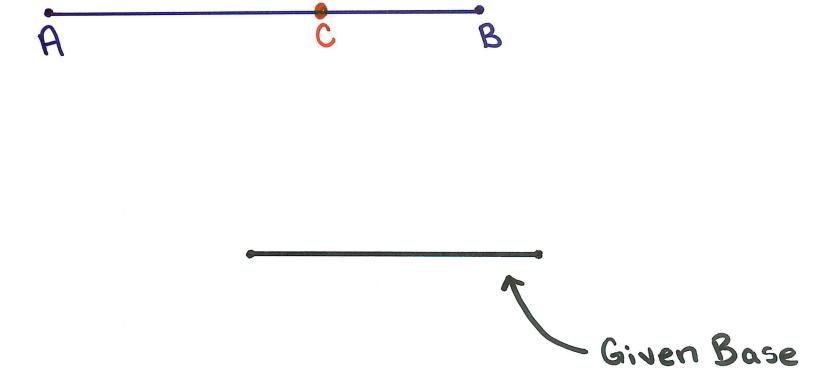




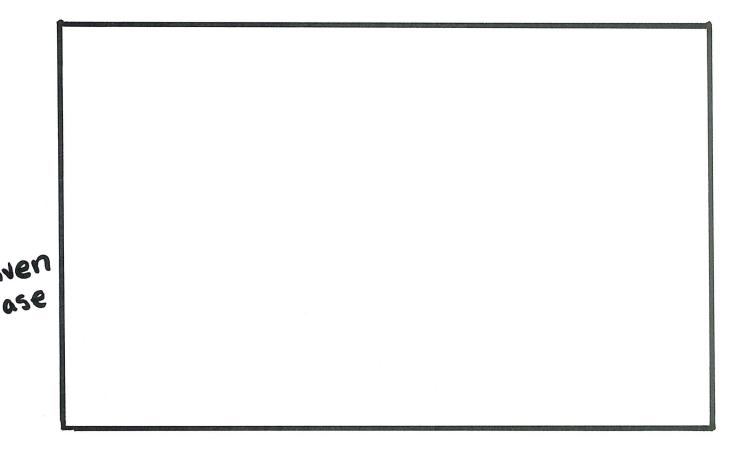
## Is This A Golden Acute Triangle?



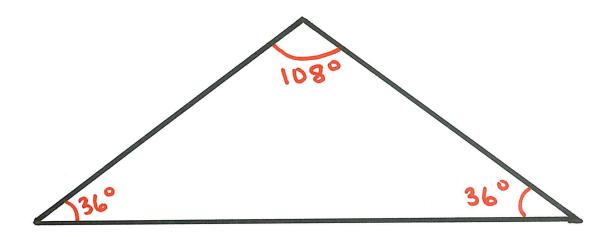
#### Construction 4: Acute Golden Triangle Over A Given Base



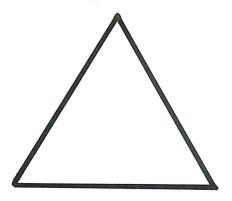
# Construction 5: Alternate Construction Of An Acute Golden Triangle Over A Given Base

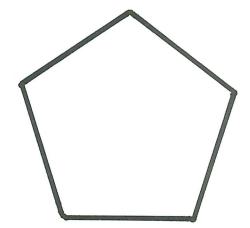


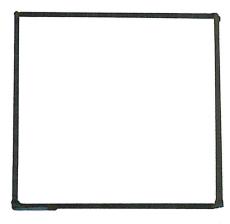
## Construction 6: Subdividing An Obtuse Golden Triangle

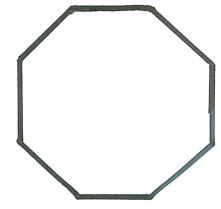


# Recall: Regular Polygons

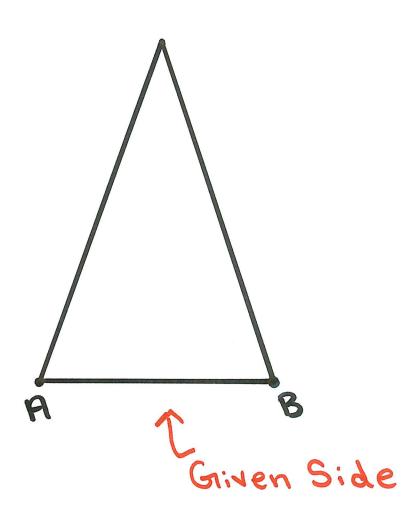


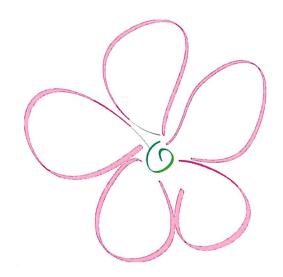






#### Construction 7: Regular Pentagon Over A Given Side





QUESTIONS???