## Problem Set 3 Due: Thursday, October 10

Work the following two problems. A subset of the problems will be graded. Be sure to adhere to the expectations outlined in the Problem Set Guidelines Sheet.

1. Find the missing digit in each of the following UPC numbers.
(a) $8-5357 m-00114-6$
(b) $m-70330-50367-0$
(c) $0-13803-1065 m-1$
2. Every book has assigned to it an International Standardized Book Number, or ISBN for short. This is a 10 -digit number and can usually be found on the back of the book. The first 9 digits contain information about the book - typically the first digit represents the language of the country in which the book was published, the next 4 represent the publisher, and the next 4 are assigned to that particular book by the publisher. The last digit is a check digit, and it is determined by the values of the first 9 digits. The idea is that a computer can be programmed to check to see if a potential ISBN is valid. This means, for example, if a clerk is typing an ISBN into a computer and makes a mistake, usually the computer will beep, announcing an error has occurred. Here is how the check digit is determined. Let $a_{1}, \ldots, a_{9}$ be the first 9 digits of an ISBN number. Then the 10 -th digit $a_{10}$ (the check digit!) is chosen so that

$$
a_{1}+2 a_{2}+\cdots+9 a_{9}+10 a_{10} \equiv 0 \quad(\bmod 11)
$$

A 10-digit number with digits $a_{1}, \ldots, a_{10}$ is called $I S B N$ valid if this congruence equation holds.
(a) Sometimes you'll come across a book whose ISBN ends in " X " rather than a digit. For example, your textbook Elementary Number Theory, Second Edition by Underwood Dudley has ISBN 0-486-46931-X. What does the X mean?
(b) Suppose Alice and Bob were at a coffee shop one day discussing books, and Bob wrote down on a napkin the ISBN for a book he thought Alice would enjoy. Unfortunately, Alice put her coffee cup on the napkin and smudged one of the digits of Bob's ISBN. What she has left is $0-8218-51 ? 4-1$, where ? is the smudged digit. Determine the value of the missing digit. Then find the title and publisher of the book which Bob recommended to Alice. (Hint: Most library search engines can search for a book by its ISBN. Some search engines want spaces rather than dashes; others want just the numbers with no spaces or dashes.)

