

## Section 1.3: The Golden Ratio

Ancient Greek mathematicians were also philosophers & artists, & the aesthetic aspects of their work was important to them.

A characteristic that makes many objects visually pleasing is their **proportionality**.

A particular proportion that is seen in ancient & modern times & all over the world is the "**golden proportion**".

Ex// Find the golden cut if AB is, say,  
7cm

**EXAMPLE 1 : CONSTRUCTING A GOLDEN CUT**

with ONLY ruler & compass, how can we  
find C given line segment AB?

**EXAMPLE 2**: CONSTRUCT A GOLDEN RECTANGLE  
(with a given height)

The golden ratio appears in ancient art & architecture. It has also been said that people's perception of beauty of a human face is closely related to whether or not it fits nicely into a (vertical) golden rectangle.

## **EXAMPLE 3: CONSTRUCT A GOLDEN SPIRAL**



Some Terminology:

Isosceles triangle:

Acute triangle:

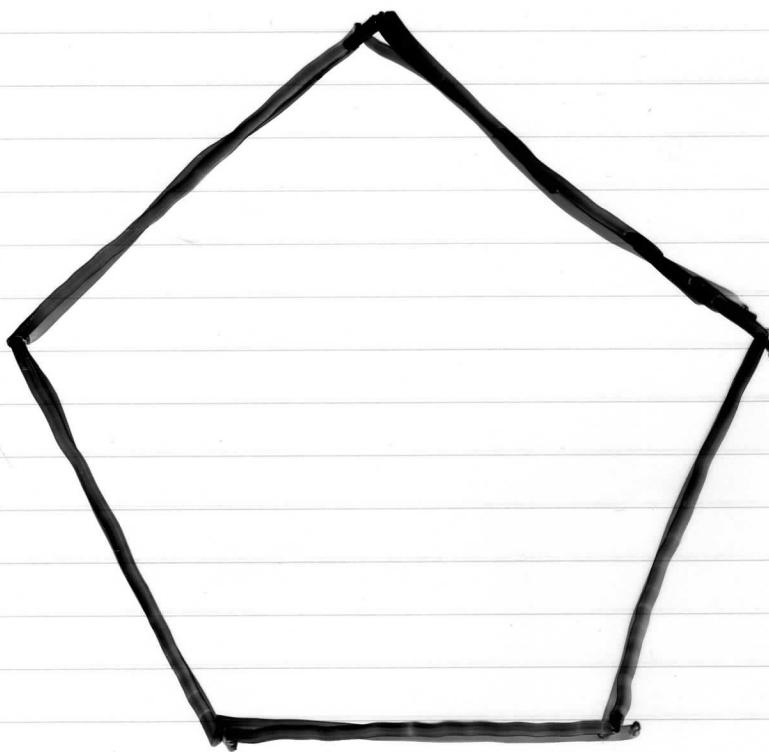
Obtuse triangle:

A "golden triangle" has the ratio of its long side over its short side = 1.618...

**EXAMPLE 4: CONSTRUCT AN ACUTE GOLDEN TRIANGLE**

we can subdivide an obtuse golden triangle into an acute & obtuse golden triangle.

# Regular Pentagon :



## EXAMPLES: CONSTRUCT A REGULAR PENTAGON

So in summary, we have seen 5 shapes made with the golden cut  $\frac{1+\sqrt{5}}{2} \approx 1.618$

- ① Golden rectangle
- ② Golden spiral
- ③ Golden Acute Triangle
- ④ Golden Obtuse Triangle
- ⑤ Regular Pentagon

## Section 1.4: Fibonacci Numbers

From the ancient Greeks we fast-forward to Italy in the middle ages, where a man named Leonardo Pisano posed this problem:

"A certain man put a pair of rabbits in a place surrounded on all sides by a wall. How many pairs of rabbits can be produced from that pair in a year if it is supposed that every month each pair begets a new pair which from the second month on becomes productive"

Leonardo lived in Bonacci, hence his moniker "**Fibonacci**" (son of Bonacci).

The increasing sequence of numbers of pairs of rabbits is the "**Fibonacci Sequence**" & the numbers in that sequence are "**Fibonacci numbers**"

This is not the most convenient formula.  
What if we wanted  $f_{150}$ ? Must start from  $f_1$ ,

ex/ find  $f_{20}$  &  $f_{21}$  given  $f_{19} = 4181$  &  $f_{22} = 17711$

The Fibonacci #'s & the golden ratio  
have a surprising & interesting relationship.

Seeds are distributed in a spiraling pattern, one set clockwise, the other counterclockwise.

Flower: how do they "arrange" seeds?

- real flowers don't like angles of displacement that go evenly into  $360^\circ$ ? Why?